

Simplified method for calculating the induced settlements and the liquefaction rate in a soil profile under seismic loading

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Overview of the Project



Objective :

Developing two predictors, one quantifies the risk of liquefaction and the other gives an estimate of the earthquake-induced settlements in a dam or a foundation under seismic loading.

Input Data:

- Time accelerogram: a seismic event characterized by its magnitude and its distance from the site is selected from a corresponding set of seismic signals in the EDF RESORCE database;
- Geometry and characteristics of the material constituting a structure (dam or foundation);
- Results of cyclic tests experimented on this material to calibrate the parameters of the chosen constitutive model.

Validation

- Transient analysis :
 - Equivalent linear analysis of a soil column with post-treatment using the Sawicki model;
 - Nonlinear analysis of a homogeneous soil column using the Hujeux model;
- Real measurements of instrumented dams.

Summary

- I. Pore pressure build up computation by a transient analysis
 - Soil profiles
 - Compaction/Liquefaction model By Sawicki
 - Equivalent linear analysis of a soil column with post-treatment using the Sawicki model;
 - Nonlinear analysis of a homogeneous soil column using the Hujieux model;
- II. 2D model of Aratozawa dam

I. Simplified estimation of the pore pressure build up under seismic loading

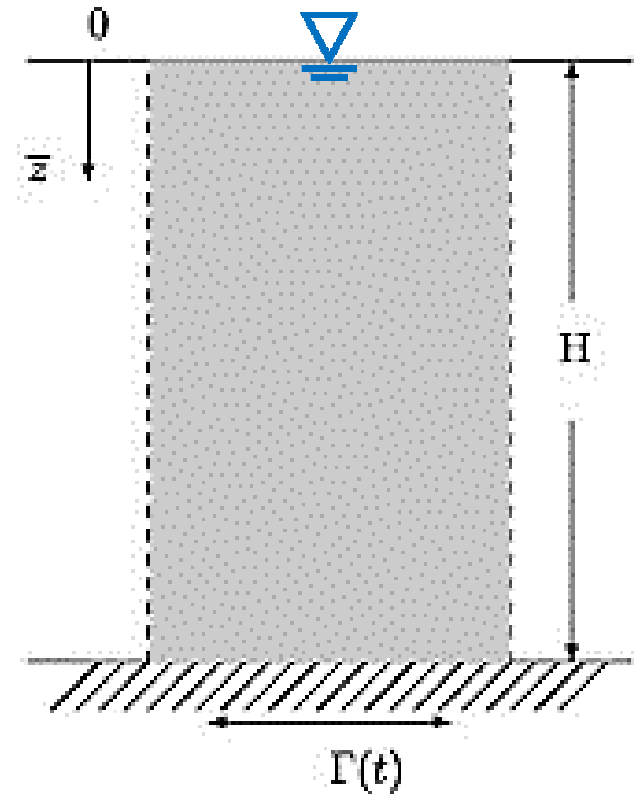
1. SOIL PROFILES UNDER CONSIDERATION

The soil profile under consideration has a thickness $H = 10$ m and overlies a bedrock regarded as perfectly rigid and subjected to a horizontal acceleration.

We will be studying three types of soil profile in the following :

- Profile 1 :
 - Loose sand with specific saturated density $\rho = 2105 \text{ Kg/m}^3$.
 - G is assumed to be constant throughout the soil profile.
- Profile 2 :
 - Loose sand with specific saturated density $\rho = 2105 \text{ Kg/m}^3$.
 - G is assumed to be a function of \sqrt{z} throughout the soil profile.
- Profile 3 :
 - Heterogeneous profile : Loose and dense sand layers.

- Sawicki Parameters $C_1 = 0,009$ et $C_2 = 55000$.



I. Simplified estimation of the pore pressure build up under seismic loading

2. Objective of the study

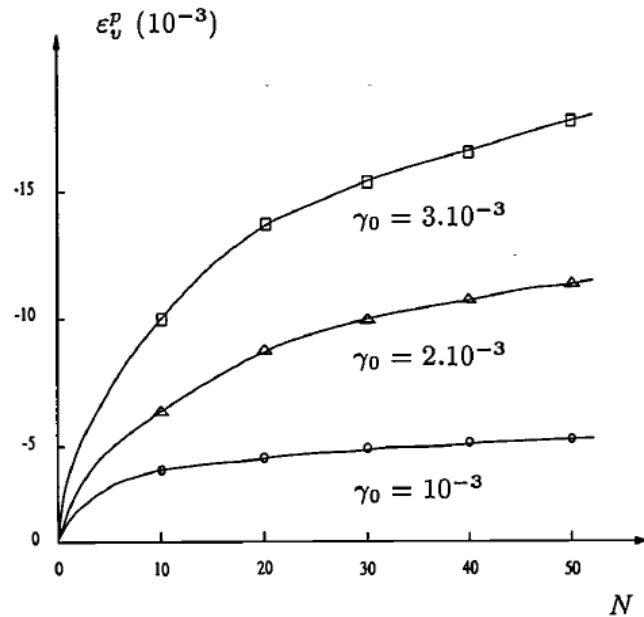
we aim this study to **predict the settlement and the liquefaction rate** in a soil profile under a horizontal seismic motion applied at the bedrock.

We choose 65 acceleregrams recorded with a PGA ranging between 0,03g and 0,54g

- As a way to validate the predictor, we compute the liquefaction rate by a transient analysis +Sawicki
→ 65 values of calculated liquefaction rates ;
- We will build the liquefaction predictor based on :
 - Profile features;
 - Sawicki's constitutive model;
 - Response spectrum and duration of input motion→ 65 values of predicted liquefaction rates ;

Compaction / Liquefaction model by SAWICKI, (1987-1989):

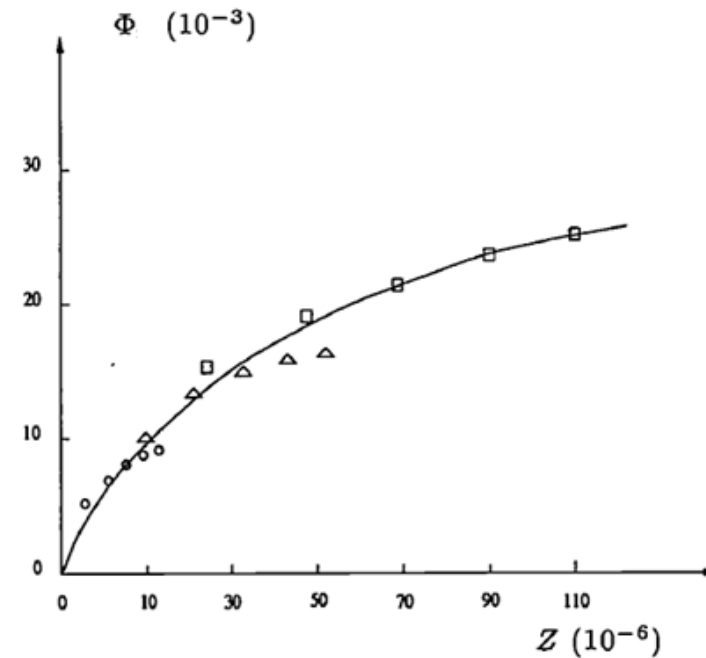
1. Compaction model (Sawicki, 1987)



Sawicki et al. (1989)

$$\Phi = \frac{1 - n_0}{n_0} \epsilon_v^p, Z = \frac{1}{4} \gamma_0^2 N$$

Φ : the relative compaction
 n_0 : the initial porosity
 ϵ_v^p : volumetric deformation



Sawicki et al. (1989)

Relative compaction :

$$\Phi = C_1 \ln(1 + C_2 Z)$$

Where C_1 and C_2 are the parameters of Sawicki's model depending on the sand and its given initial relative density.

Compaction / Liquefaction model by SAWICKI, (1987-1989):

2. Liquefaction model (Sawicki, 1989)

Sawicki model also provides a method to assess the generation of pore pressure under cyclic loading:

$$\frac{du}{dN} = \frac{1}{a} \frac{d\Phi}{dN} \quad \Rightarrow \quad \frac{du}{dN} = K \frac{d\varepsilon_v^p}{dN}$$

where u is the pore pressure.

a is a constant calculated using: $a = \frac{1-n_0}{n_0} k_s$

with n_0 the initial porosity, k_s the elastic compressibility of the soil $k_s = \frac{1}{K}$ and K is the compression modulus

So if we already know the variation of the relative porosity in cycles (volumetric deformations), we can find the generation of pressure.

Otherwise, Sawicki proposed a formula that derives directly the pore pressure build up from the shear strain, which reads:

$$\frac{du}{dN} = \frac{D_1 \gamma^2}{4a} \exp(-D_2 au)$$

D_1 and D_2 are deduced from C_1 and C_2

I. Pore pressure build up computation by a transient analysis

Step 1

Linear equivalent computation

We have launched an equivalent linear computation on the EDF software Code_Aster.

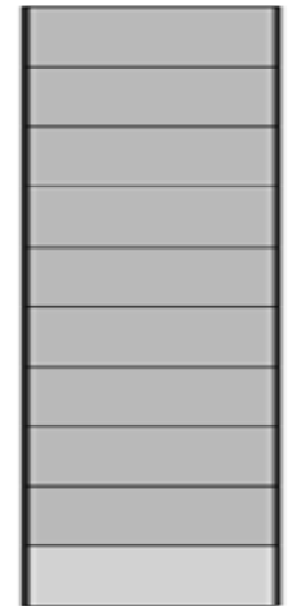
The calculation requires the following information as input data:

- A table containing the geotechnical characteristics of each layer: density, initial Young's modulus, Poisson coefficient, initial hysteretic damping.
- The degradation curves of the modulus of shear and damping for the material used.

LAYER 1

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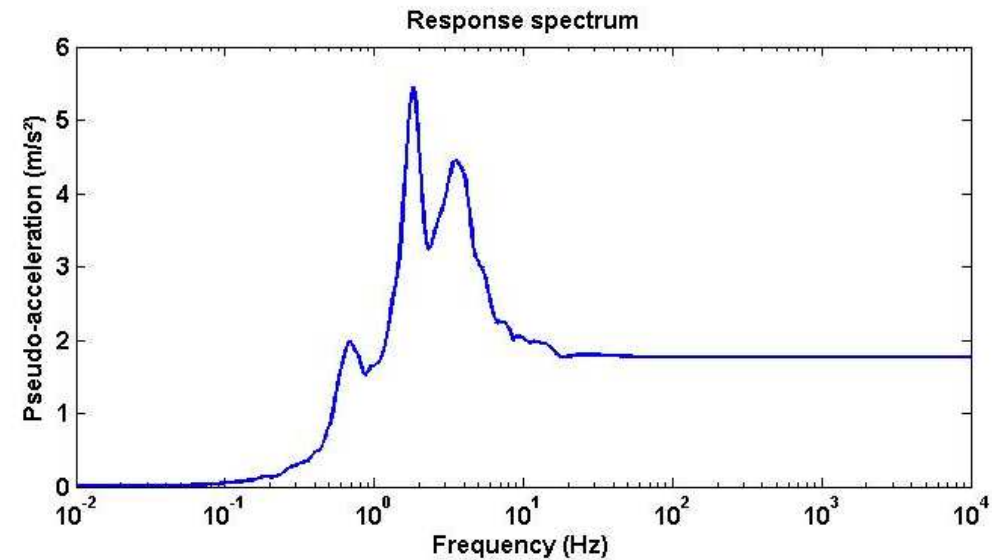
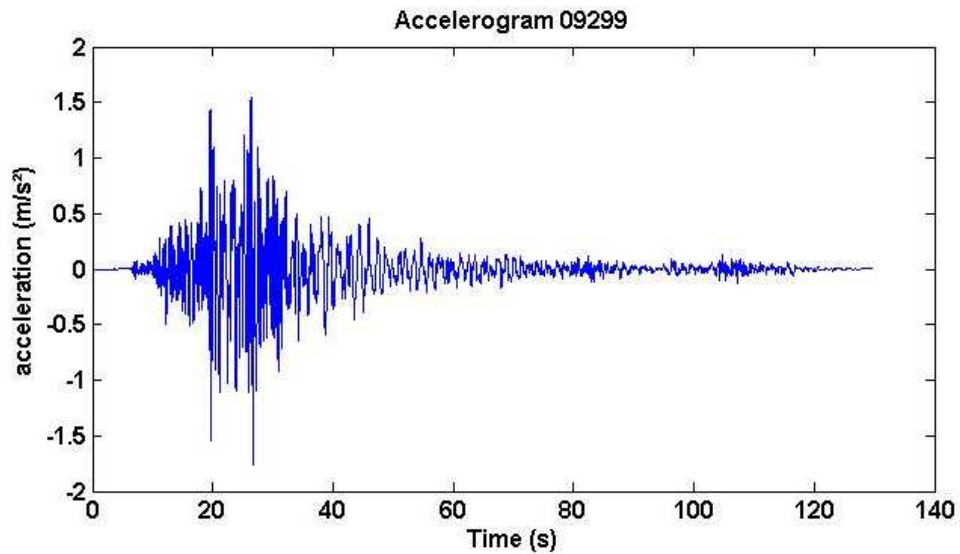
LAYER 9
BEDROCK



↔
 $\Gamma(t)$

I. Pore pressure build up computation by a transient analysis

Input signal:



Earthquake's name	Mw	Distance (km)	a _{max} (g)	Strong phase duration (s)
Razan 09299	6.4	24	0,176	28,52

I. Pore pressure build up computation by a transient analysis

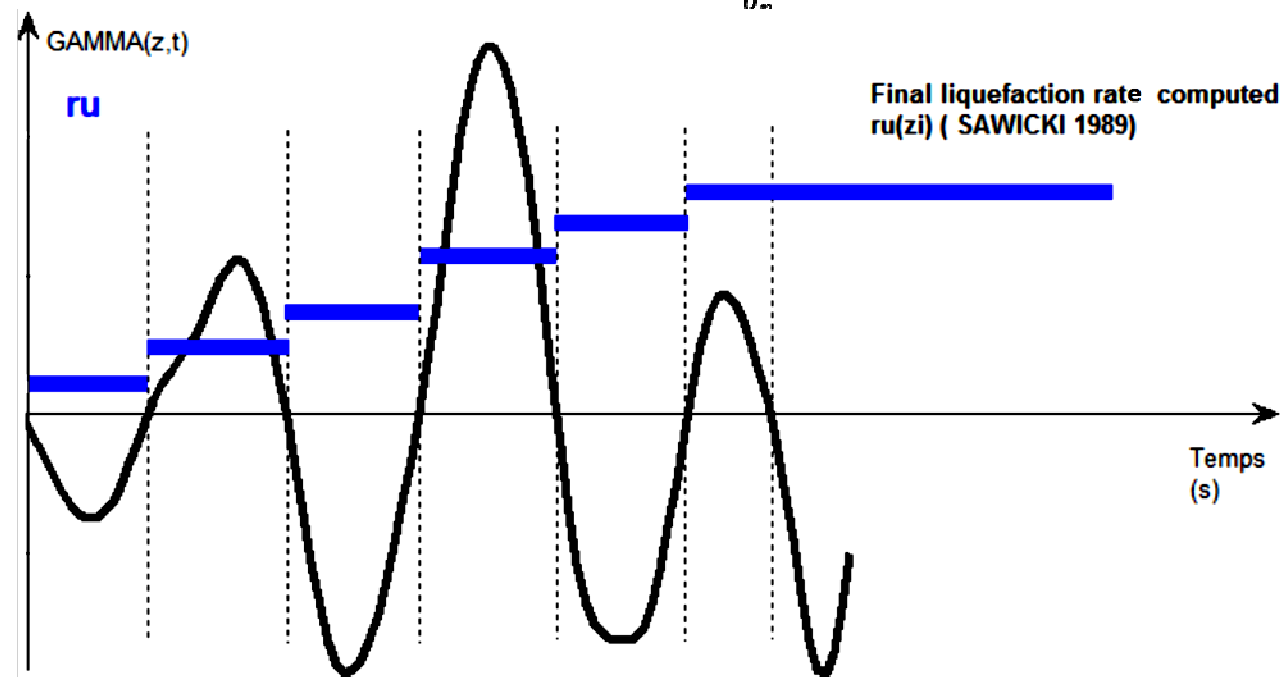
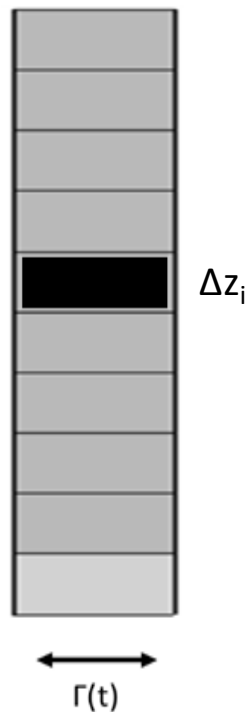
Step 2

- The Sawicki liquefaction model is used to calculate the pore pressure rise following the history of the shear strain
- For each layer i (Δz_i), the shear strain time history is decomposed into a succession of half-cycles.
- Each half-cycle contributes to the value of:

$$\text{Volumetric deformation increment: } \Delta \varepsilon_v (\text{half-cycle}) = \frac{n_o}{1-n_o} \times C_1 \times \ln(1 + C_2 (\frac{1}{4} \gamma_{max}^2)^{\frac{1}{2}})$$

$$\text{Pore pressure rise : } \Delta u_{(\text{half-cycle})} = K \times \Delta \varepsilon_v$$

$$\text{Liquefaction rate at the depth } z : r_{u i} = \frac{\Delta u}{\sigma'_v}$$



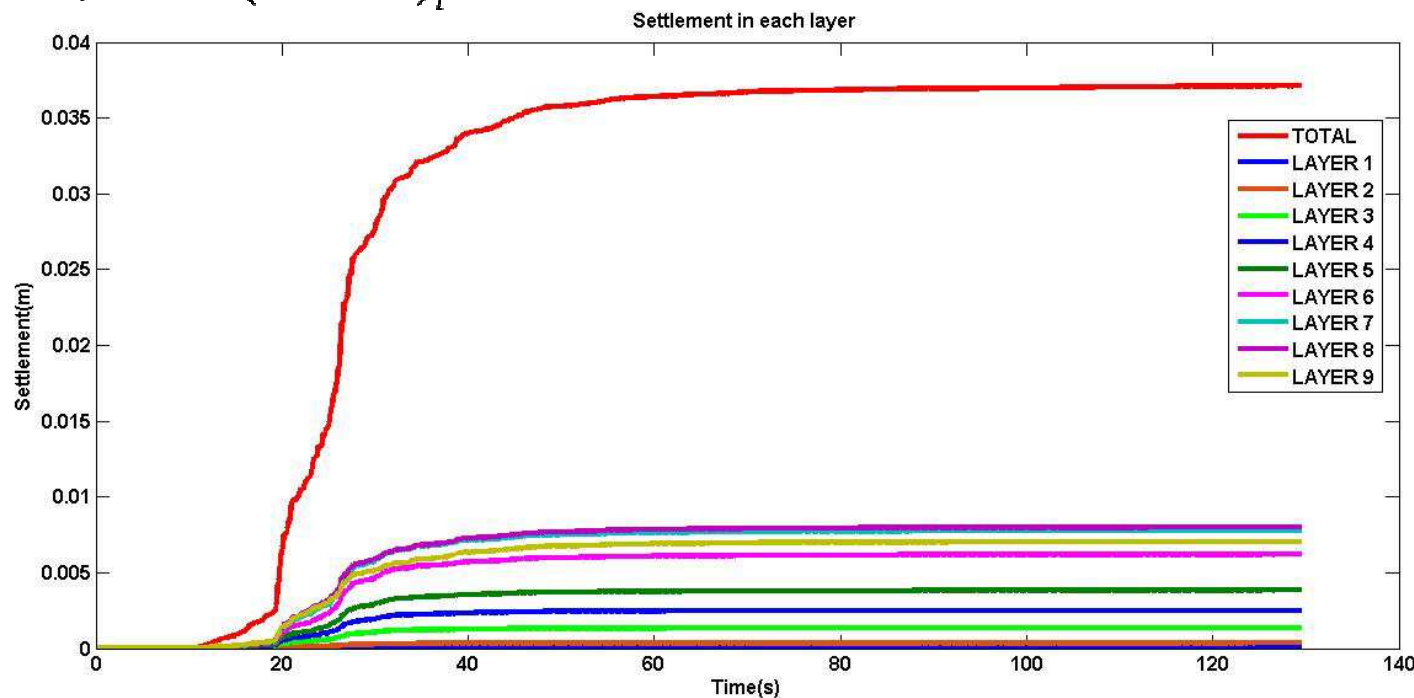
I. Pore pressure build up computation by a transient analysis

Settlement computation

- To compute the settlement induced in each layer, the volumetric deformation generated at the end of the signal is taken up in each layer i:

Volumetric deformation increment: $\Delta\varepsilon_v (half-cycle) = \frac{n_o}{1-n_o} \times C_1 \times \ln(1 + C_2(\frac{1}{4}\gamma_{max}^2)^{\frac{1}{2}})$

Settlement in each layer $S_i = (\varepsilon_v(t_{final}))_i \times \Delta z_i$

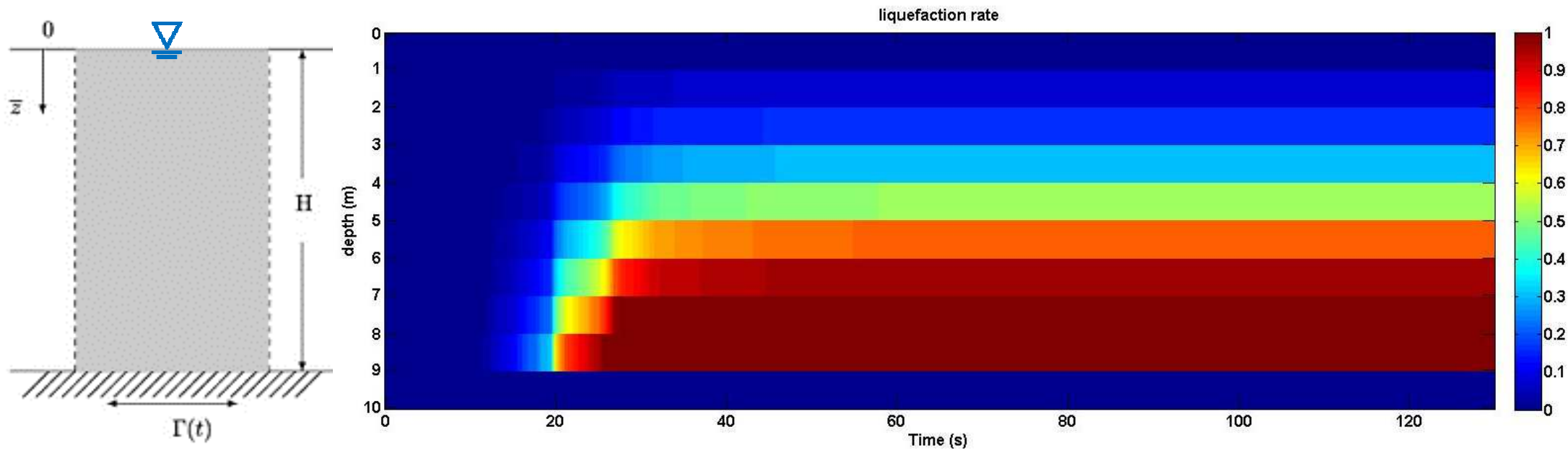


The total settlement in the entire profile is the sum of the settlements in all layers= $\sum_i S_i$

I. Pore pressure build up computation by a transient analysis

Output: liquefaction rate

Profile 1 (G assumed constant in the entire profile)

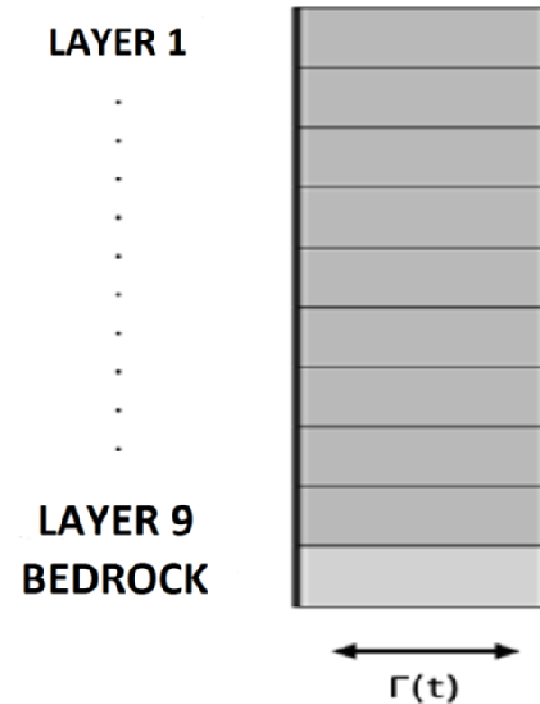


I. Pore pressure build up computation by a transient analysis

Profile 2 of soil column

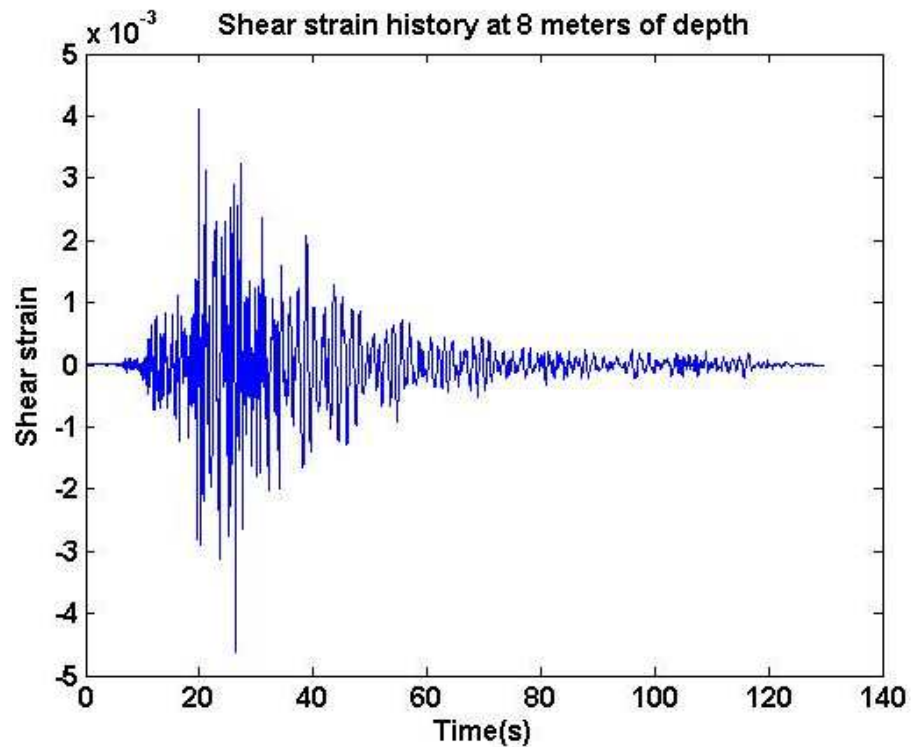
❖ the Young's modulus is a function of \sqrt{z}

Layer	RHO	E_{\max} (MPa)
Layer 1	2105	70
Layer 2	2105	99
Layer 3	2105	122
Layer 4	2105	140
Layer 5	2105	157
Layer 6	2105	172
Layer 7	2105	186
Layer 8	2105	199
Layer 9	2105	211
Layer 10	2365	5 600



I. Pore pressure build up computation by a transient analysis

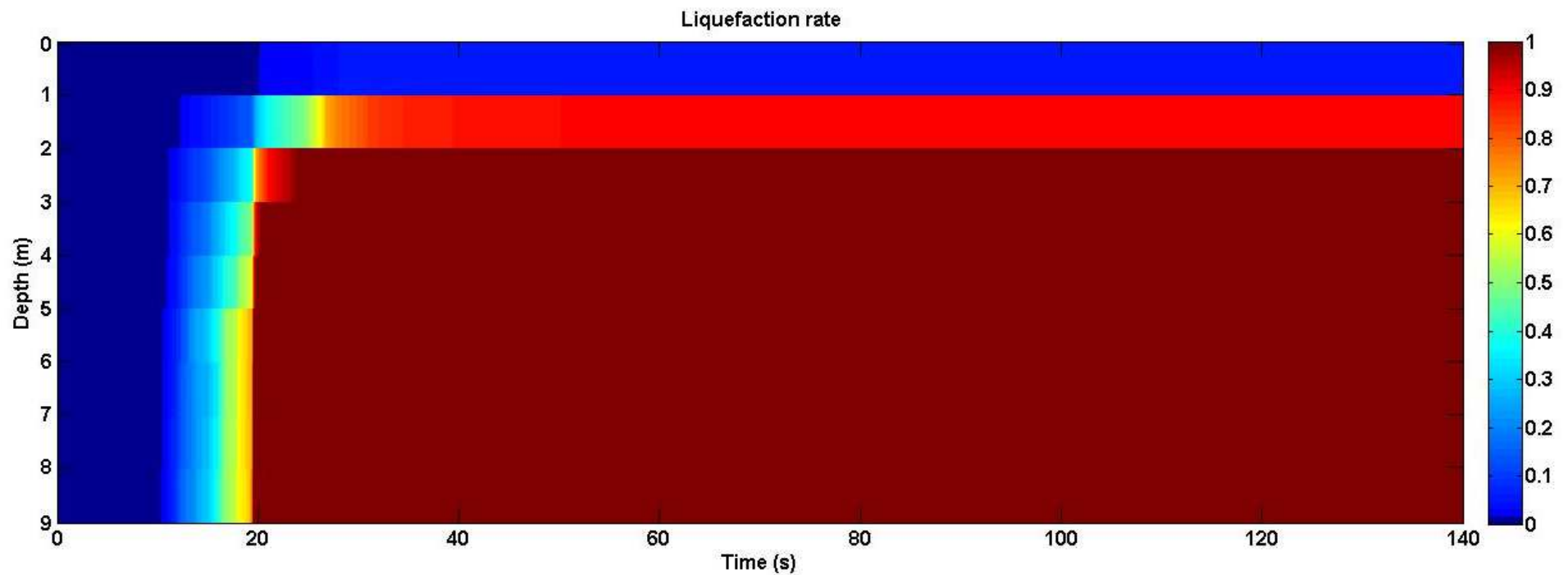
Output of the linear equivalent computation of the profile 2



Layer	G/Gmax	γ_{\max}
Layer 1	0,45	1,51E-04
Layer 2	0,16	8,08E-04
Layer 3	0,11	1,56E-03
Layer 4	0,09	2,14E-03
Layer 5	0,07	2,78E-03
Layer 6	0,06	3,85E-03
Layer 7	0,05	4,53E-03
Layer 8	0,05	4,63E-03
Layer 9	0,05	4,24E-03
Layer 10	1,00	0

I. Pore pressure build up computation by a transient analysis

Profile 2: Liquefaction rate



I. Pore pressure build up computation by a transient analysis

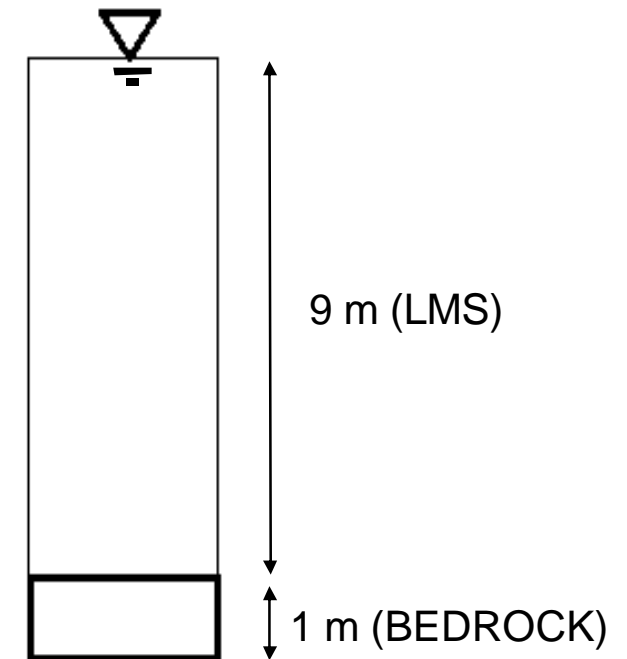
Nonlinear computation of the profile 2 response

A nonlinear calculation was performed on a column of soil under undrained conditions using the Hujeux model embedded in Code Aster, as a way to validate the computation that we use (linear equivalent + Sawicki)

The column is composed of a loose sand, and has the same elastic characteristic as the one studied previously.

Boundary conditions:

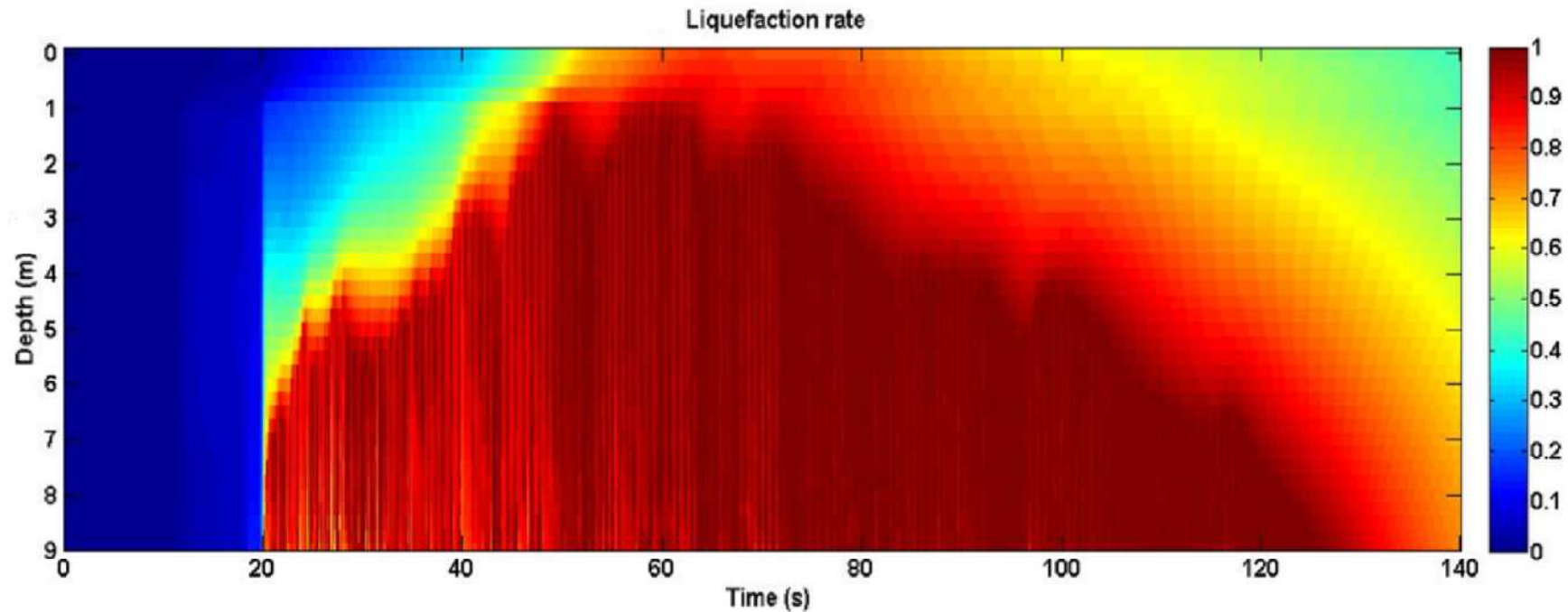
- Absorbing borders at bedrock;
 - Periodicity conditions on the lateral sides;
- And the Seismic signal is imposed as a plane wave loading



I. Pore pressure build up computation by a transient analysis

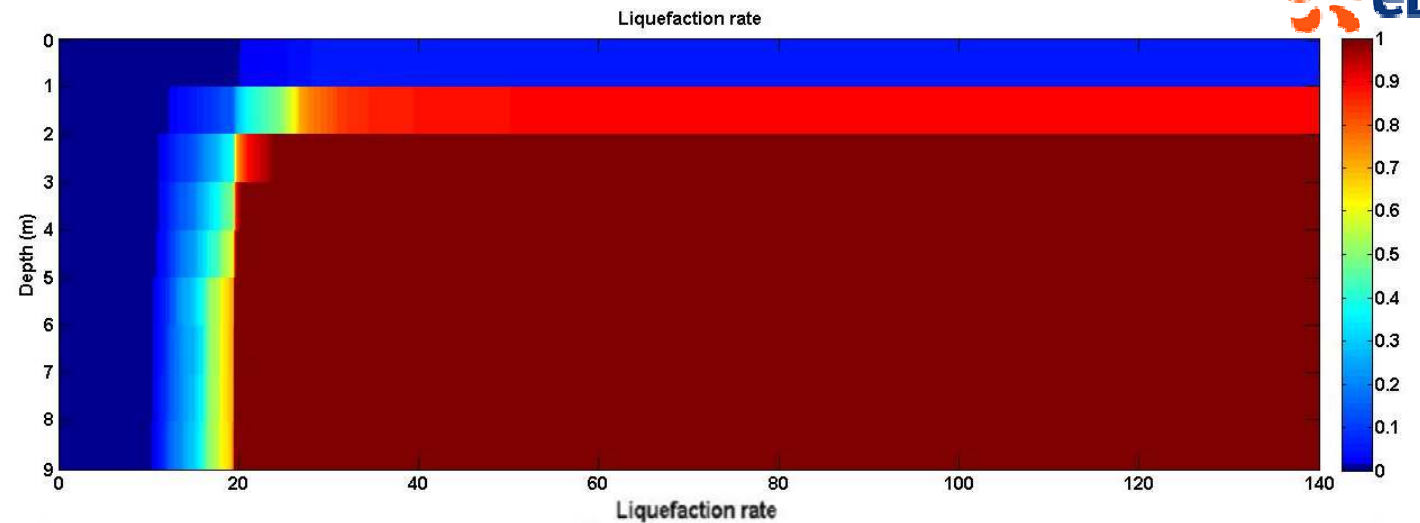
Nonlinear computation of the profile 2 response

Profile 2: Liquefaction rate

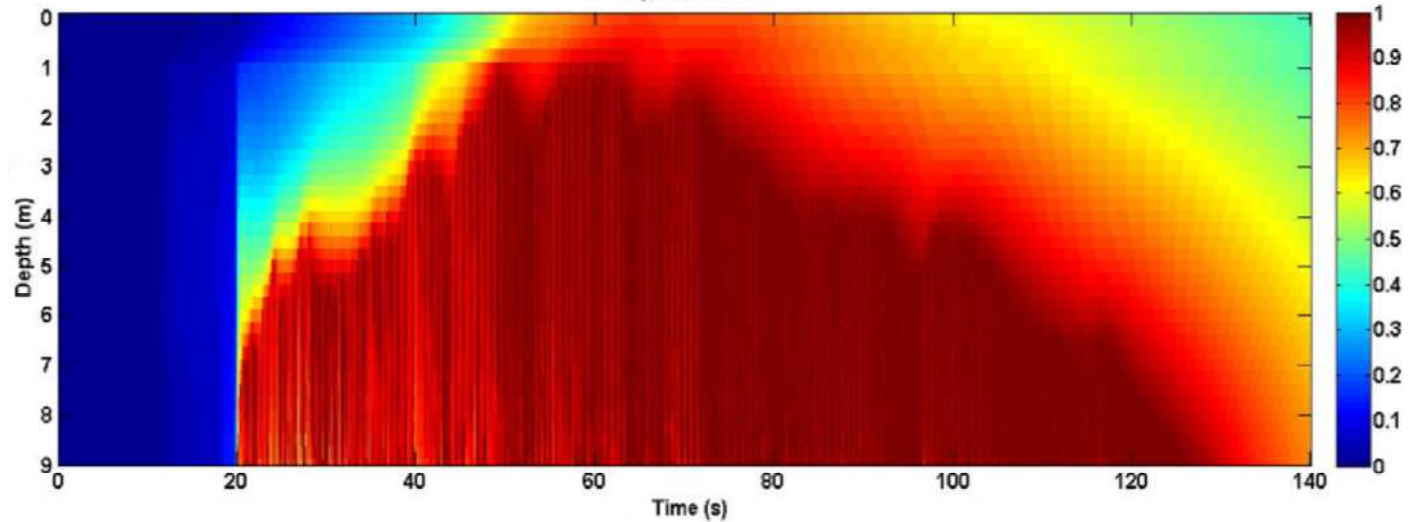


Comparing the two methods : linear equivalent computation + Sawicki and the non linear computation for the profile 2

Linear equivalent computation + Sawicki



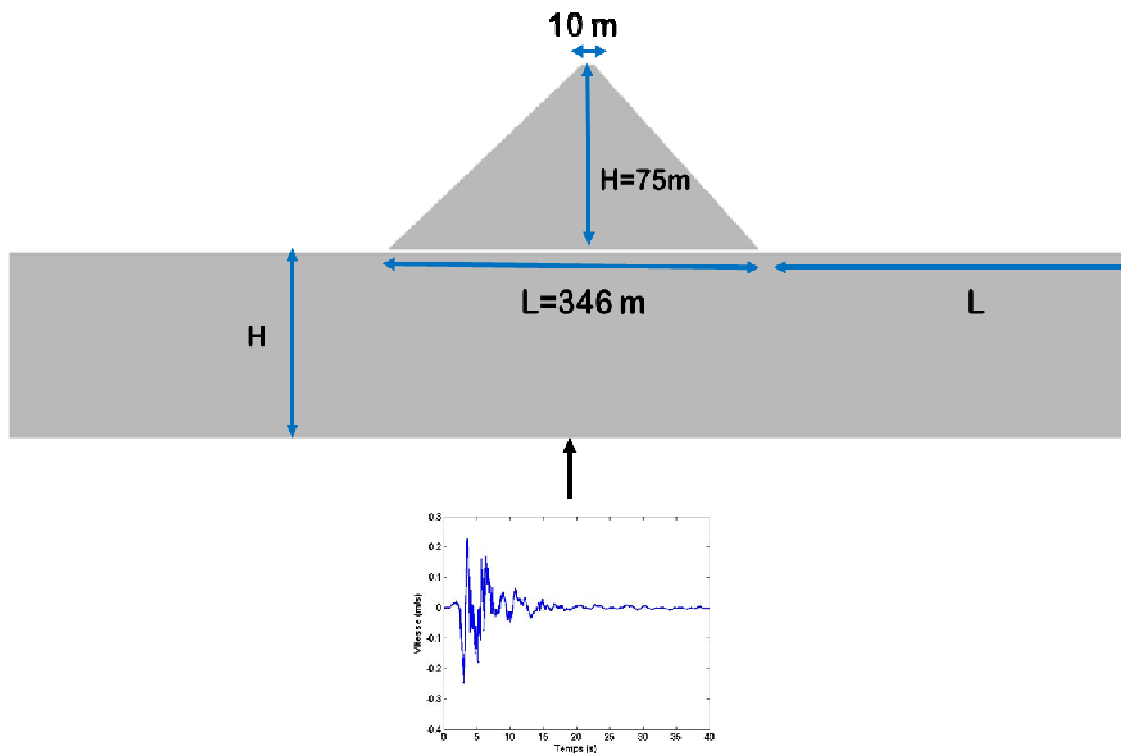
Non linear computation (Hujeux)



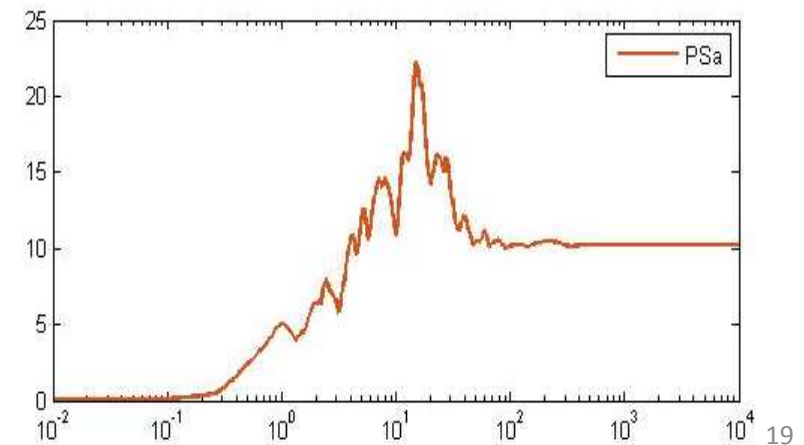
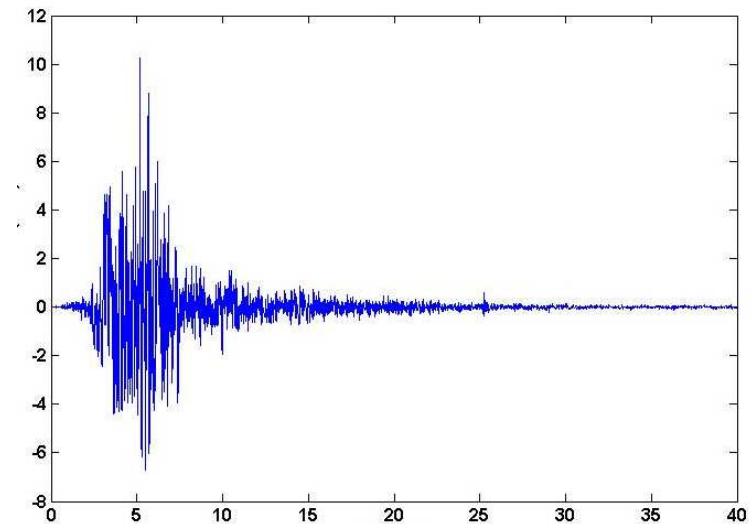
III. 2D Model of Aratozawa dam

The main objective of our project is to build a pore pressure predictor that allows us to estimate the liquefaction risk in a dam under seismic loading.

So in the next part of our work we will be extending our method to consider a 2D dam model

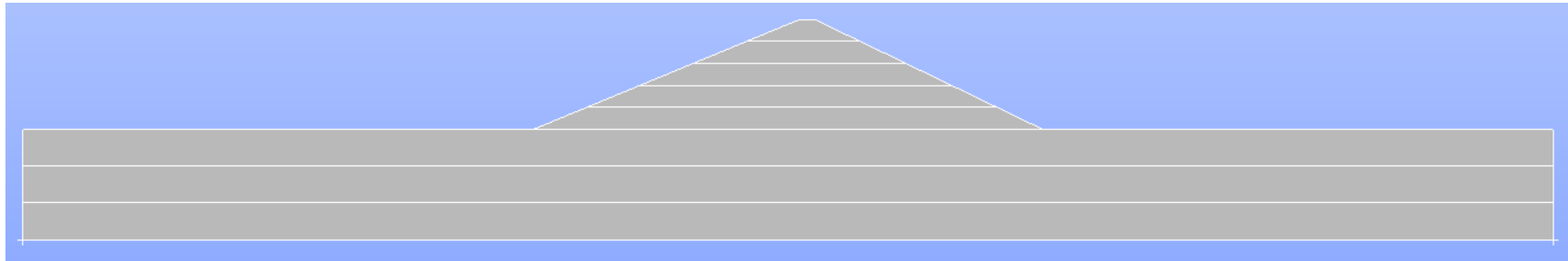


Accelerogram of the 2008- earthquake

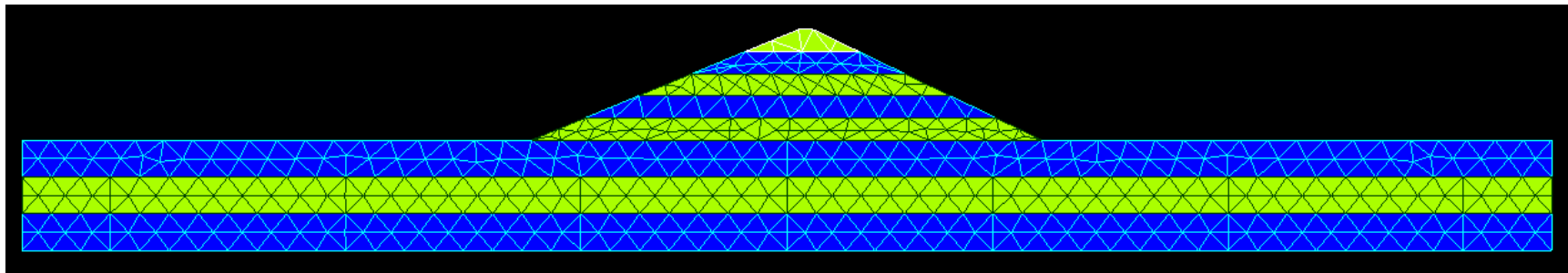


III. 2D Model of Aratozawa dam

Dividing the dam model to layers

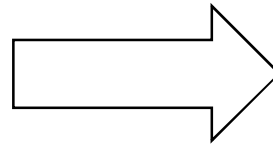


And each layer is meshed



III. 2D Model of Aratozawa dam : coupled analysis

- Linear calculation for each layer and calculate the shear strain history in each layer.
- Post-treatment with the Sawicki model to calculate the rise of pore pressure.
- Update of the characteristics of the layer: G/G_{max} by considering the degradation soil curves and the impact of the pore pressure rise.
- Repeat the linear calculation with the new features in an iterative way until reaching the convergence.



The distribution of the liquefaction rate in the entire dam

AFTER developing the validation method, we proceed to build our liquefaction and settlement predictors.

Thank you for your attention