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DIRECT METHOD FOR DYNAMIC SOIL-STRUCTURE INTERACTION BASED ON SEISMIC INERTIA FORCES

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Shaping a Better Energy Future

Direct method for dynamic soil-structure interaction based on seismic inertia forces



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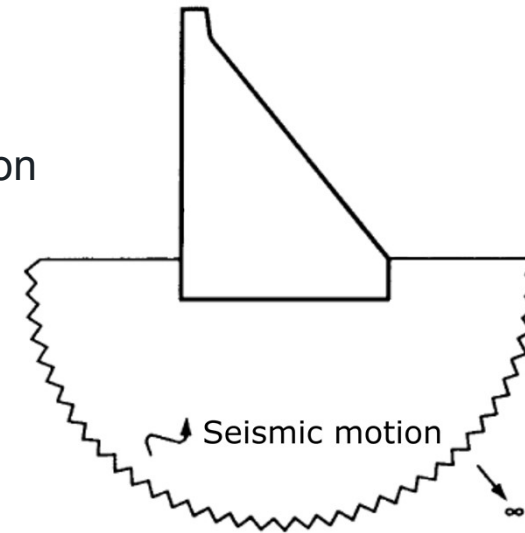
- 1) Soil-Structure Interaction
- 2) FEM formulation of SSI problems
- 3) Equivalence of Direct Method and Substructure Method
- 4) Numerical validation
- 5) Conclusions

Soil-Structure Interaction (SSI)



Context and Motivation

- **Dynamic Soil-Structure Interaction (SSI)**
 - Vibrations of the structure interact with seismic motion
 - High impact on seismic response of dams
- **SSI FEM modelling critical issues**
 - Semi-unbounded size of foundation medium
 - How and where imposing seismic excitation
- **Standard massless method**
 - FEM modelling of limited portion of foundation medium with no mass
 - Straightforward implementation within commercial FEM software
 - Wave propagation and radiation damping into foundation are ignored
 - Application of design surface ground motion at model bottom boundary
 - Unphysical numerical results leading to dam stress overestimation
- **Need of more accurate approaches for SSI in common commercial FEM codes**



FEM formulation of SSI problems



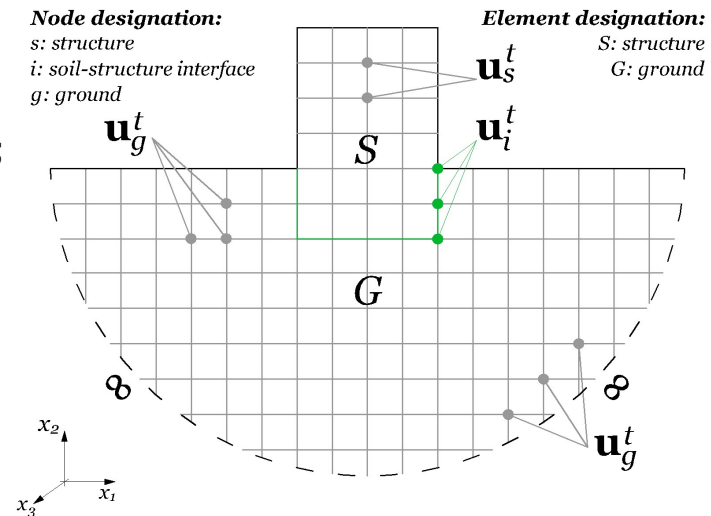
Governing equations in total displacements (u^t)

TIME DOMAIN:

$$\begin{bmatrix} \mathbf{M}_{ss}^S & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{M}_{ii}^{S+G} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{M}_{gg}^G \end{bmatrix} \begin{Bmatrix} \ddot{\mathbf{u}}_s^t \\ \ddot{\mathbf{u}}_i^t \\ \ddot{\mathbf{u}}_g^t \end{Bmatrix} + \begin{bmatrix} \mathbf{K}_{ss}^S & \mathbf{K}_{si}^S & \mathbf{0} \\ \mathbf{K}_{is}^S & \mathbf{K}_{ii}^{S+G} & \mathbf{K}_{ig}^G \\ \mathbf{0} & \mathbf{K}_{gi}^G & \mathbf{K}_{gg}^G \end{bmatrix} \begin{Bmatrix} \mathbf{u}_s^t \\ \mathbf{u}_i^t \\ \mathbf{u}_g^t \end{Bmatrix} = \begin{Bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{Bmatrix};$$

FREQUENCY DOMAIN:

$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S & \mathbf{0} \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^{S+G} & \bar{\mathbf{K}}_{ig}^G \\ \mathbf{0} & \bar{\mathbf{K}}_{gi}^G & \bar{\mathbf{K}}_{gg}^G \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s^t \\ \bar{\mathbf{u}}_i^t \\ \bar{\mathbf{u}}_g^t \end{Bmatrix} = \begin{Bmatrix} \mathbf{0} \\ \mathbf{0} \\ \mathbf{0} \end{Bmatrix}; \quad \bar{\mathbf{K}}_{kl} = \mathbf{K}_{kl} - \omega^2 \mathbf{M}_{kl};$$



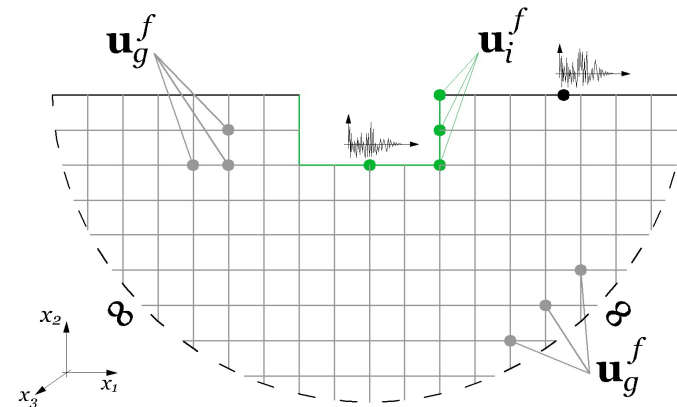
Governing equations of free-field input motion (u^f)

u^f : site response that would have occurred before placing the structure on the site

FREQUENCY DOMAIN:

$$\begin{bmatrix} \bar{\mathbf{K}}_{ii}^G & \bar{\mathbf{K}}_{ig}^G \\ \bar{\mathbf{K}}_{gi}^G & \bar{\mathbf{K}}_{gg}^G \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_i^f \\ \bar{\mathbf{u}}_g^f \end{Bmatrix} = \begin{Bmatrix} \mathbf{0} \\ \mathbf{0} \end{Bmatrix};$$

$$\mathbf{K}_{ss}^S \bar{\mathbf{u}}_s^f + \mathbf{K}_{si}^S \bar{\mathbf{u}}_i^f = \mathbf{0}; \quad (\text{Pseudo-static transmission})$$



FEM formulation of SSI problems

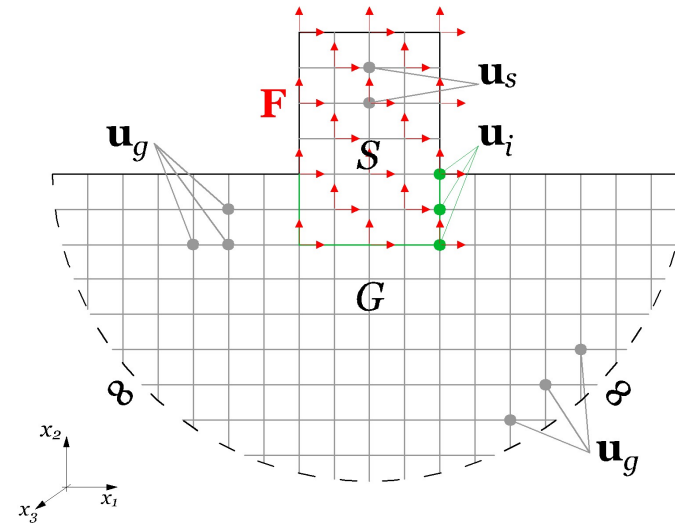


Governing equations in relative displacements (\mathbf{u})

$\mathbf{u} = \mathbf{u}^t - \mathbf{u}^f$: relative/interaction response, i.e. the amount of the total response due to the interaction effects induced by the presence of the structure;

$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S & \mathbf{0} \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^{S+G} & \bar{\mathbf{K}}_{ig}^G \\ \mathbf{0} & \bar{\mathbf{K}}_{gi}^G & \bar{\mathbf{K}}_{gg}^G \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s \\ \bar{\mathbf{u}}_i \\ \bar{\mathbf{u}}_g \end{Bmatrix} = - \begin{Bmatrix} -\omega^2 \mathbf{M}_{ss}^S \bar{\mathbf{u}}_s^f \\ \bar{\mathbf{K}}_{is}^S \bar{\mathbf{u}}_s^f + \bar{\mathbf{K}}_{ii}^S \bar{\mathbf{u}}_i^f \\ \mathbf{0} \end{Bmatrix};$$

Remark: dynamic stiffness submatrices $\bar{\mathbf{K}}_{ig}^G$, $\bar{\mathbf{K}}_{gi}^G$ and $\bar{\mathbf{K}}_{gg}^G$ have theoretically infinite dimensions;



Uniform free-field assumption

$$\bar{\mathbf{u}}^f = \begin{Bmatrix} \bar{\mathbf{u}}_s^f \\ \bar{\mathbf{u}}_i^f \\ \bar{\mathbf{u}}_g^f \end{Bmatrix} = \begin{bmatrix} \mathbf{I} & \mathbf{0} \\ \mathbf{I} & \mathbf{0} \\ \mathbf{0} & \mathbf{I} \end{bmatrix} \begin{bmatrix} \mathbf{r}_i^{x_1} & \mathbf{r}_i^{x_2} & \mathbf{r}_i^{x_3} \\ \mathbf{r}_g^{x_1} & \mathbf{r}_g^{x_2} & \mathbf{r}_g^{x_3} \end{bmatrix} \begin{Bmatrix} \mathbf{v}_{x_1}^f \\ \mathbf{v}_{x_2}^f \\ \mathbf{v}_{x_3}^f \end{Bmatrix};$$

$$\bar{\mathbf{K}}_{is}^S \bar{\mathbf{u}}_s^f + \bar{\mathbf{K}}_{ii}^S \bar{\mathbf{u}}_i^f = -\omega^2 \mathbf{M}_{ii};$$

$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S & \mathbf{0} \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^{S+G} & \bar{\mathbf{K}}_{ig}^G \\ \mathbf{0} & \bar{\mathbf{K}}_{gi}^G & \bar{\mathbf{K}}_{gg}^G \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s \\ \bar{\mathbf{u}}_i \\ \bar{\mathbf{u}}_g \end{Bmatrix} = - \begin{Bmatrix} -\omega^2 \mathbf{M}_{ss}^S \bar{\mathbf{u}}_s^f \\ -\omega^2 \mathbf{M}_{ii}^S \bar{\mathbf{u}}_i^f \\ \mathbf{0} \end{Bmatrix};$$

The exciting dynamic forces are the product of the free-field acceleration and the inertial properties of the structure

Equivalence of DM and SM



$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S & \mathbf{0} \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^{S+G} & \bar{\mathbf{K}}_{ig}^G \\ \mathbf{0} & \bar{\mathbf{K}}_{gi}^G & \bar{\mathbf{K}}_{gg}^G \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s \\ \bar{\mathbf{u}}_i \\ \bar{\mathbf{u}}_g \end{Bmatrix} = - \begin{Bmatrix} -\omega^2 \mathbf{M}_{ss}^S \bar{\mathbf{u}}_s^f \\ \bar{\mathbf{K}}_{is}^S \bar{\mathbf{u}}_s^f + \bar{\mathbf{K}}_{ii}^S \bar{\mathbf{u}}_i^f \\ \mathbf{0} \end{Bmatrix};$$

Dynamic condensation of soil dofs:

$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^S + \mathbf{S}_{ii}^G \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s \\ \bar{\mathbf{u}}_i \end{Bmatrix} = - \begin{Bmatrix} -\omega^2 \mathbf{M}_{ss}^S \bar{\mathbf{u}}_s^f \\ \bar{\mathbf{K}}_{is}^S \bar{\mathbf{u}}_s^f + \bar{\mathbf{K}}_{ii}^S \bar{\mathbf{u}}_i^f \end{Bmatrix};$$

SUBSTRUCTURE METHOD (SM) IN RELATIVE COMPONENTS

$\mathbf{S}_{ii}^G = \bar{\mathbf{K}}_{ii}^G + \bar{\mathbf{K}}_{ig}^G \bar{\mathbf{K}}_{gg}^{G^{-1}} \bar{\mathbf{K}}_{gi}^G$: dynamic impedance matrix of the unbounded soil region, calculated by a *semi-analytical solution*;

By substituting $\mathbf{u}^t = \mathbf{u} + \mathbf{u}^f$ the more familiar SM in total displacements is retrieved

$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^S + \mathbf{S}_{ii}^G \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s^t \\ \bar{\mathbf{u}}_i^t \end{Bmatrix} = \begin{Bmatrix} \mathbf{0} \\ \mathbf{S}_{ii}^G \bar{\mathbf{u}}_i^f \end{Bmatrix};$$

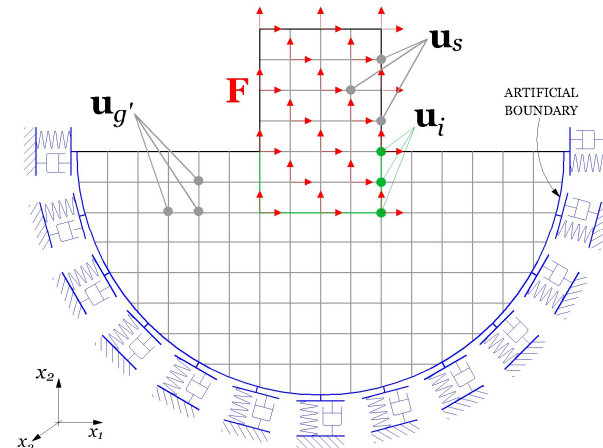
$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S & \mathbf{0} \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^{S+G} & \bar{\mathbf{K}}_{ig'}^{G'} \\ \mathbf{0} & \bar{\mathbf{K}}_{g'i}^{G'} & \bar{\mathbf{K}}_{g'g'}^{G'} \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s \\ \bar{\mathbf{u}}_i \\ \bar{\mathbf{u}}_{g'} \end{Bmatrix} = - \begin{Bmatrix} -\omega^2 \mathbf{M}_{ss}^S \bar{\mathbf{u}}_s^f \\ \bar{\mathbf{K}}_{is}^S \bar{\mathbf{u}}_s^f + \bar{\mathbf{K}}_{ii}^S \bar{\mathbf{u}}_i^f \\ \mathbf{0} \end{Bmatrix};$$

Dynamic condensation of soil dofs:

$$\begin{bmatrix} \bar{\mathbf{K}}_{ss}^S & \bar{\mathbf{K}}_{si}^S \\ \bar{\mathbf{K}}_{is}^S & \bar{\mathbf{K}}_{ii}^S + \bar{\mathbf{S}}_{ii}^{G'} \end{bmatrix} \begin{Bmatrix} \bar{\mathbf{u}}_s \\ \bar{\mathbf{u}}_i \end{Bmatrix} = - \begin{Bmatrix} -\omega^2 \mathbf{M}_{ss}^S \bar{\mathbf{u}}_s^f \\ \bar{\mathbf{K}}_{is}^S \bar{\mathbf{u}}_s^f + \bar{\mathbf{K}}_{ii}^S \bar{\mathbf{u}}_i^f \end{Bmatrix};$$

DIRECT METHOD (DM) IN RELATIVE COMPONENTS

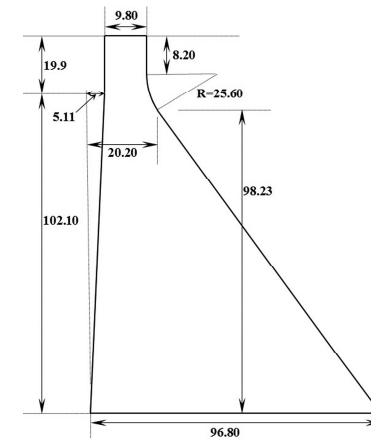
$\bar{\mathbf{S}}_{ii}^{G'} = \bar{\mathbf{K}}_{ii}^{G'} + \bar{\mathbf{K}}_{ig'}^{G'} \bar{\mathbf{K}}_{g'g'}^{G'^{-1}} \bar{\mathbf{K}}_{g'i}^{G'}$: dynamic impedance matrix of the truncated soil model with transmitting boundaries;



Numerical validation



Case study: Pine Flat Dam

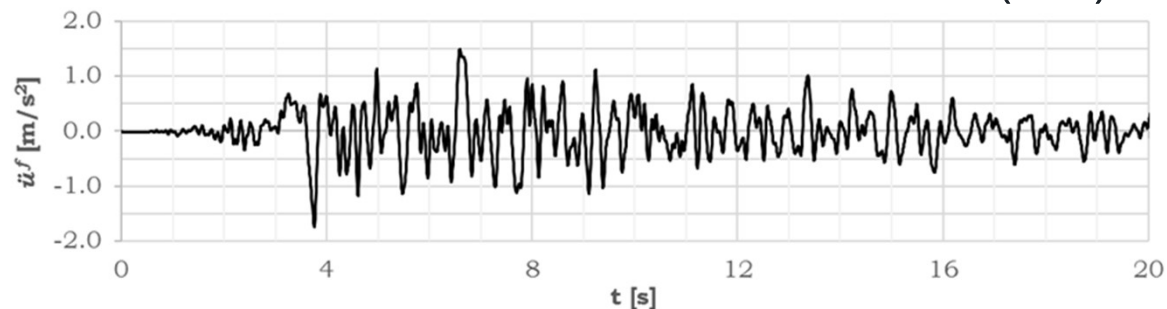


REFERENCE MECHANICAL PROPERTIES OF THE SYSTEM

	Concrete	Rock
Dynamic Young's modulus [GPa]	22.41	68.95
Dynamic Poisson's ratio [1]	0.20	0.33
Mass density [kg/m ³]	2483	2643
Hysteretic damping factor	0.1	0.1

$$\bar{K}_{kl} = K_{kl}(1 + i\eta) - \omega^2 M_{kl};$$

S69E HORIZONTAL COMPONENT OF TAFT GROUND ACCELERATION (1952)

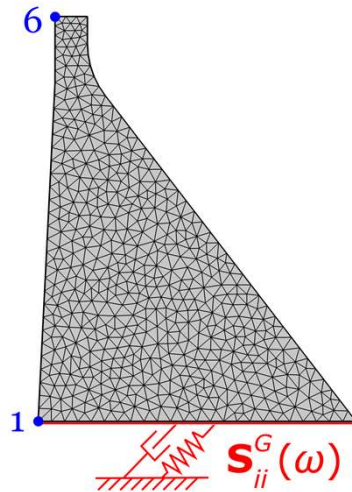


Numerical validation



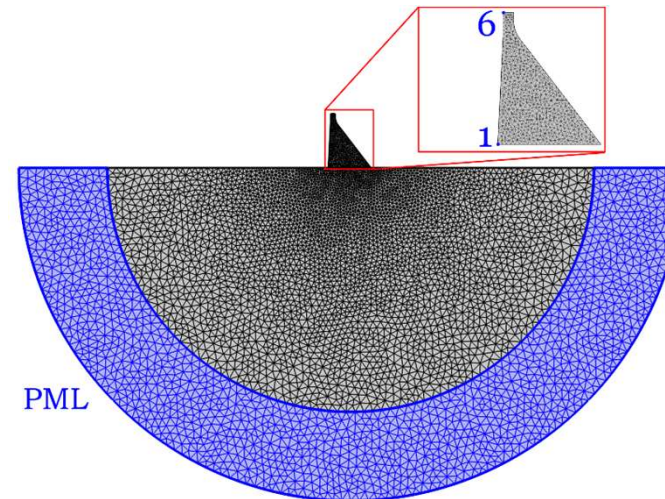
Computational models

SUBSTRUCTURE METHOD



- Autonomous implementation of SM in MATLAB
- Semi-analytical solution for $S_{ii}^G(\omega)$
- Frequency Domain analysis
- 972 elements, 536 nodes

DIRECT METHOD



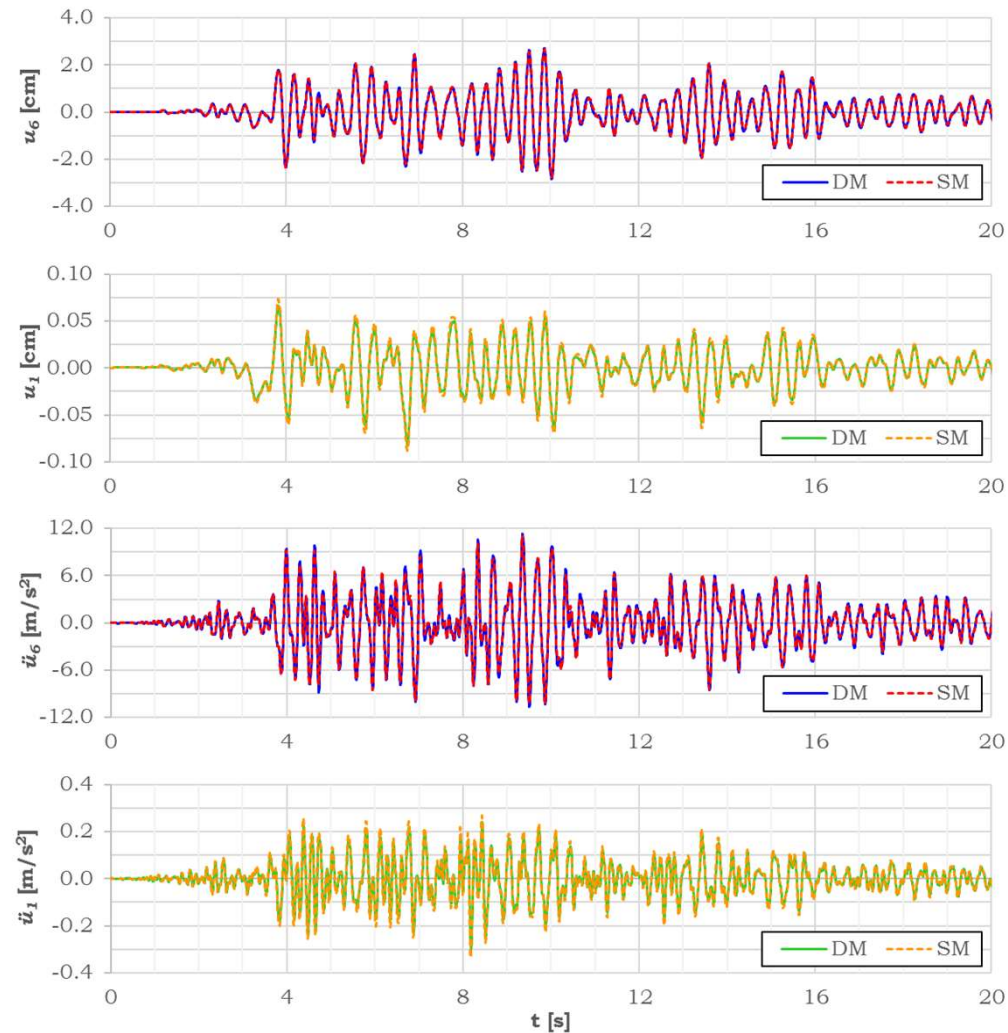
- FEM modelization of DM within COMSOL Multiphysics
- PML transmitting boundary
- Frequency Domain analysis
- 10275 elements, 5284 nodes

Linear triangular FEs; Frequency range= [0, 50] Hz, $\Delta f = 0.012$ Hz

Numerical validation



Results



Conclusions



- Implementation of an alternative version of Direct Method for including SSI effects in seismic analysis of dams
- In case of for uniform free-field motion, the seismic action is modelled by inertial loads applied on the dam only
- Simple implementation within commercial FEM software
- Comparison assessment with respect to widespread SM to verify the rigour of adopted DM
- Exact equivalence between DM and SM, if consistently implemented
- Perfect match of numerical results on benchmark problem of Pine Flat Dam gathered from both methods, confirming exact theoretical derivations



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Thank you for your kind attention



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